## **BSTA 200 - TEST 1 FORMULA SHEET**

### Nature of data

Qualitative data, quantitative data (continuous or discrete)

#### Levels of Measurement

nominal level, ordinal level, interval level, ratio level

# Organization of data

Frequency table, relative frequency, cumulative frequency

Relative Frequency = 
$$\frac{class\ frequency}{sum\ of\ frequencies}$$

Number of intervals - use the  $2^k$  rule,  $2^k > n$  (sample size) where k = number of intervals

Class width = 
$$\frac{range}{k}$$
 or  $\frac{range}{\# of intervals}$ 

Class Midpoint = 
$$\frac{sum\ of\ two\ consecutive\ lower\ limits}{2}$$

# **Measures of Location (Measures of Central Tendency)**

	Population data	Sample data
Arithmetic Mean	$\mu = \frac{\sum x}{N}$	$\bar{x} = \frac{\sum x}{n}$
Position of Median	$\frac{N+1}{2}$	$\frac{n+1}{2}$
Mode	Most frequent observation	
Weighted Mean	$\frac{\sum w(x)}{\sum w}$ where w = weighting factor $x = \text{individual value}$	

Last revision: June, 2016

### **Measures of Variation (spread)**

	Population data	Sample data
Range	Highest value – lowest value	
Mean Absolute Deviation	$\frac{\sum  x - \mu }{N}$	$\frac{\sum  x - \overline{x} }{n}$
Standard deviation	$\sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}$	$s = \sqrt{\frac{\sum (x - \overline{x})^2}{n - 1}}$ $s = \sqrt{\frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1}}$
Variance	$\sigma^2$	$s^2$
Coefficient of Variation (CV)	$CV = \frac{\sigma}{\mu}$	$\mathbf{CV} = \frac{s}{\overline{x}}$

### Measures of position: deciles, quartiles, percentiles

Location of percentile  $L_p = (n+1)\frac{P}{100}$ ,

where n = number of observations in the data set, L = position of designated percentile in data set and P = desired percentile

# **Correlation and Regression**

 $Total\ Variation = Regression\ Sum\ of\ Squares + Error\ Sum\ of\ Squares$ 

$$SST = SSR + SSE$$

Coefficient of Correlation (r) 
$$r = \frac{n\sum xy - (\sum x)(\sum y)}{\sqrt{[n(\sum x^2) - (\sum x)^2][n(\sum y^2) - (\sum y)^2]}}$$

Coefficient of Determination (
$$\mathbb{R}^2$$
)  $R^2 = \frac{explained\ variation}{total\ variation}$  or  $\frac{SSR}{SST}$ 

Standard Error of Estimate 
$$s_e = \sqrt{\frac{\sum y^2 - a(\sum y) - b(\sum xy)}{n-2}}$$
 or  $\sqrt{\frac{SSE}{n-2}}$ 

**Regression Equation**  $\hat{y} = a + bx$ 

where 
$$b = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$
 and  $a = \frac{\sum y}{n} - b \frac{\sum x}{n}$ 

Last revision: June, 2016