

Calculating Percentiles
Statistics

P_p is the p^{th} percentile of the data

L_p is the locator variable for P_p

n is the size of the data set

$$L_p = (n + 1) \times \frac{p}{100} \quad (\text{the location of } P_p \text{ within the data set})$$

For the ordered data set 1 7 12 12 15 15 19 $n = 7$.

Example 1: The 75th percentile, P_{75} , is found as follows:

$$L_{75} = (7 + 1) \times \frac{75}{100} = (8) \times 0.75 = 6 \quad \text{A WHOLE NUMBER}$$

1 7 12 12 15 15 19 Since 15 is the 6th element, then $P_{75} = 15$.

Example 2: The 30th percentile, P_{30} , is found as follows:

$$L_{30} = (7 + 1) \times \frac{30}{100} = (8) \times 0.3 = 2.4 = \begin{array}{c} 2 \\ \downarrow \\ 2^{\text{nd}} \\ \text{element} \end{array} + \begin{array}{c} 0.4 \\ \downarrow \\ 40\% \text{ of the way from} \\ \text{the } 2^{\text{nd}} \text{ to } 3^{\text{rd}} \text{ element} \end{array} \quad \text{A DECIMAL NUMBER}$$

2.4 is between the 2nd element and the 3rd element

1 7 12 12 15 15 19

$$\begin{aligned} P_{30} &= 2^{\text{nd}}\text{element} + [0.4 \times (3^{\text{rd}}\text{element} - 2^{\text{nd}}\text{element})] \\ &= 7 + [(0.4) \times (12 - 7)] \\ &= 7 + [0.4 \times (5)] \\ &= 7 + 2 \\ &= 9 \end{aligned}$$

Therefore, $P_{30} = 9$.

