

TMAT 102
MID-TERM EXAM FORMULA SHEET

CHAPTER 1: Numerical Computation

Distance = Rate \times Time

Amount = Rate \times Base (where rate is in decimal form)

$$\% \text{ change} = \frac{\text{new value} - \text{original value}}{\text{original value}} \times 100 \quad \% \text{ error} = \frac{\text{Measured Value} - \text{Known value}}{\text{Known value}} \times 100$$

$$\% \text{ efficiency} = \frac{\text{output}}{\text{input}} \times 100 \quad \% \text{ conc. of A} = \frac{\text{Amount of A}}{\text{Total Amount of Mixture}} \times 100$$

CHAPTER 2: Algebra

$$(a \pm b)^2 = a^2 \pm 2ab + b^2 \quad a^2 - b^2 = (a - b)(a + b)$$

Given nonzero real numbers x and y , and integers m and n :

$$x^1 = x \quad x^0 = 1 \quad x^{-n} = \frac{1}{x^n}$$

$$(x^m)^n = x^{mn} \quad x^m \cdot x^n = x^{m+n} \quad \frac{x^m}{x^n} = x^{m-n}$$

$$(xy)^n = x^n y^n \quad \left(\frac{x}{y}\right)^n = \frac{x^n}{y^n} \quad \left(\frac{x}{y}\right)^{-n} = \left(\frac{y}{x}\right)^n$$

CHAPTER 7: Right Triangles and Vectors

$$1 \text{ rev} = 360^\circ = 2\pi \text{ radians} \quad 1^\circ = 60' \quad 1' = 60'' \quad 1 \text{ rad} \approx 57.3^\circ$$

Given $(x,y) \neq (0,0)$ on terminal arm of angle θ , let $r = \sqrt{x^2 + y^2}$, then,

$$\sin(\theta) = \frac{y}{r} \quad \cos(\theta) = \frac{x}{r} \quad \tan(\theta) = \frac{y}{x}$$

$$\csc(\theta) = \frac{1}{\sin(\theta)} \quad \sec(\theta) = \frac{1}{\cos(\theta)} \quad \cot(\theta) = \frac{1}{\tan(\theta)}$$

$$c^2 = a^2 + b^2 \text{ (Pythagorean Theorem)}$$

$$\sin(\theta) = \frac{\text{opp}}{\text{hyp}} \quad \cos(\theta) = \frac{\text{adj}}{\text{hyp}} \quad \tan(\theta) = \frac{\text{opp}}{\text{adj}}$$

CHAPTER 15: Oblique Triangles and Vectors

$$\csc \theta = \frac{1}{\sin \theta} \quad \sec \theta = \frac{1}{\cos \theta} \quad \cot \theta = \frac{1}{\tan \theta}$$

$$\sin \theta = \sin(180^\circ - \theta) \quad \cos \theta = \cos(360^\circ - \theta) \quad \tan \theta = \tan(180^\circ + \theta)$$

Law of Sines:
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Law of Cosines:

$$a^2 = b^2 + c^2 - 2bc \cos A \quad \text{or} \quad \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$
$$b^2 = a^2 + c^2 - 2ac \cos B \quad \text{or} \quad \cos B = \frac{a^2 + c^2 - b^2}{2ac}$$
$$c^2 = a^2 + b^2 - 2ab \cos C \quad \text{or} \quad \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

CHAPTER 16: Radian Measure, Arc Length and Rotation

$$1 \text{ rev} = 360^\circ = 2\pi \text{ radians}$$

Arc Length:
$$\theta = \frac{S}{r} \quad (\text{where } \theta \text{ is in radians})$$

Area of a Sector:
$$A = \frac{r^2 \theta}{2} \quad (\text{where } \theta \text{ is in radians})$$

Area of a Segment:

$$A = r^2 \arccos\left(\frac{r-h}{r}\right) - (r-h)\sqrt{2rh-h^2} \quad (\text{where } \arccos\left(\frac{r-h}{r}\right) \text{ is in radians})$$