

TMTH 114
Midterm Exam Formula Sheet

Chapter 8: Factoring

$$(a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$a^2 - b^2 = (a - b)(a + b)$$

Chapter 9: Fractions

$$\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$$

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{ad}{bc}$$

Chapter 13: Exponents and Radicals

$$\sqrt[n]{a} = a^{1/n}$$

$$a^{m/n} = \sqrt[n]{a^m} = (\sqrt[n]{a})^m$$

Given nonzero real numbers x and y , and integers m and n :

$$x^1 = x$$

$$x^0 = 1$$

$$x^{-n} = \frac{1}{x^n}$$

$$(x^m)^n = x^{m \cdot n}$$

$$x^m \cdot x^n = x^{m+n}$$

$$\frac{x^m}{x^n} = x^{m-n}$$

$$(xy)^n = x^n y^n$$

$$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$$

$$\left(\frac{x}{y}\right)^{-n} = \left(\frac{y}{x}\right)^n$$

Chapter 19: Ratio, Proportion, and Variation

Direct Variation: $y = kx$ or $\frac{y_2}{y_1} = \frac{x_2}{x_1}$

Power Variation: $y = kx^n$ or $\frac{y_2}{y_1} = \frac{(x_2)^n}{(x_1)^n}$

Inverse Variation: $y = \frac{k}{x}$ or $\frac{y_2}{y_1} = \frac{x_1}{x_2}$

Joint Variation: $y = kxw$

Chapter 20: Exponential and Logarithmic Functions

Growth:

$$y = ae^{nt}$$

Decay:

$$y = ae^{-nt}$$

Growth to an Upper Limit:

$$y = a(1 - e^{-nt})$$

Exponential Form: $y = b^x$

Logarithmic Form: $\log_b y = x$

Properties of logarithms (where $b, M, N > 0$, $b \neq 1$, and p is a real number):

$$\log_b MN = \log_b M + \log_b N$$

$$\log_b \frac{M}{N} = \log_b M - \log_b N$$

$$\log_b M^p = p \cdot \log_b M$$

$$\log_b 1 = 0$$

$$\log_b b = 1$$

$$\log_b b^M = M$$

$$b^{\log_b M} = M$$

$$\log_b a = \frac{\log a}{\log b} = \frac{\ln a}{\ln b}$$

Common logarithm: $\log x = \log_{10} x$

Natural logarithm: $\ln x = \log_e x$, where $e \approx 2.718$