

TMTH 202
FINAL EXAM FORMULA SHEET

CHAPTER 11: Determinants

Cramer's Rule:

$$x = \frac{\begin{vmatrix} c_1 & b_1 \\ c_2 & b_2 \\ a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}}{\Delta} \quad y = \frac{\begin{vmatrix} a_1 & c_1 \\ a_2 & c_2 \\ a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}}{\Delta} \quad \Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix} \neq 0$$
$$x = \frac{\begin{vmatrix} k_1 & b_1 & c_1 \\ k_2 & b_2 & c_2 \\ k_3 & b_3 & c_3 \end{vmatrix}}{\Delta} \quad y = \frac{\begin{vmatrix} a_1 & k_1 & c_1 \\ a_2 & k_2 & c_2 \\ a_3 & k_3 & c_3 \end{vmatrix}}{\Delta} \quad z = \frac{\begin{vmatrix} a_1 & b_1 & k_1 \\ a_2 & b_2 & k_2 \\ a_3 & b_3 & k_3 \end{vmatrix}}{\Delta}$$

CHAPTER 12: Matrices

$$AA^{-1} = A^{-1}A = I \quad \text{and} \quad X = A^{-1}B$$

CHAPTER 14: Quadratic Equations

Quadratic Formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

CHAPTER 17: Graphs of the Trigonometric Functions

General Sine Wave: $y = a \sin(bx + c)$

amplitude = $|a|$ period = $\frac{360^\circ}{b}$ or $\frac{2\pi}{b}$ frequency = $\frac{b}{360^\circ}$ or $\frac{b}{2\pi}$

phase angle = c phase shift = $-\frac{c}{b}$ $\cos \theta = \sin(\theta + 90^\circ)$

Sine Wave as a Function of Time t: $y = a \sin(\omega t + \phi)$

amplitude = $|a|$ angular velocity = ω period = $\frac{2\pi}{\omega}$

frequency = $\frac{\omega}{2\pi}$ phase angle = ϕ phase shift = $-\frac{\phi}{\omega}$

Addition of a sine wave and cosine wave:

$$A \sin \omega t + B \cos \omega t = R \sin(\omega t + \phi) \quad \text{where}$$

$$R = \sqrt{A^2 + B^2} \quad \text{and} \quad \phi = \arctan\left(\frac{B}{A}\right)$$

Transforming between Polar and Rectangular Coordinates:

$$x = r \cos \theta \quad \text{and} \quad y = r \sin \theta$$

$$r = \sqrt{x^2 + y^2} \quad \text{and} \quad \theta = \arctan\left(\frac{y}{x}\right)$$

CHAPTER 18: Trigonometric Identities and Equations

$$\cot\theta = \frac{1}{\tan\theta} \quad \sec\theta = \frac{1}{\cos\theta} \quad \csc\theta = \frac{1}{\sin\theta} \quad \tan\theta = \frac{\sin\theta}{\cos\theta} \quad \cot\theta = \frac{\cos\theta}{\sin\theta}$$

$$\sin^2 \theta + \cos^2 \theta = 1 \quad 1 + \tan^2 \theta = \sec^2 \theta \quad 1 + \cot^2 \theta = \csc^2 \theta$$

CHAPTER 20: Exponential and Logarithmic Functions

Growth

$$y = ae^{nt}$$

Decay

$$y = ae^{-nt}$$

Growth to an Upper Limit

$$y = a(1 - e^{-nt})$$

Compound Interest

$$y = a(1 + n)^t$$

$$y = a \left(1 + \frac{n}{m}\right)^{mt}$$

Doubling Time and Half-Life

$$t = \frac{\ln 2}{n}$$

$$\log_b N = a \quad b^a = N$$

$$\log\left(\frac{M}{N}\right) = \log M - \log N$$

$$\log(MN) = \log M + \log N$$

$$\log M^n = n \log M$$

CHAPTER 22: Analytic Geometry

Straight Line

Distance formula.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Equation of Straight line (General Form)

$$Ax + By + C = 0$$

Equation of Straight line (Slope-Intercept Form)

$$y = mx + b$$

Equation of Straight line (Point-slope Form)

$$m = \frac{y - y_1}{x - x_1}$$

$$\text{or } y - y_1 = m(x - x_1)$$

Equation of Straight line (Two-point form)

$$\frac{y - y_1}{x - x_1} = \frac{y_2 - y_1}{x_2 - x_1}$$

Intersection angle between two lines

$$\tan \phi = \frac{m_2 - m_1}{1 + m_1 m_2}$$

Circle

Standard Equation (Circle of Radius r)
Centre at (h, k)

$$(x - h)^2 + (y - k)^2 = r^2$$

Parabola

Standard Equation (Vertex at origin)
Axis Horizontal

$$y^2 = 4px$$

Standard Equation (Vertex at origin)
Axis Vertical

$$x^2 = 4py$$

Focal Width

$$L = |4p|$$

Ellipse

Standard Equation (Centre at origin)
Major axis vertical

$$\frac{y^2}{a^2} + \frac{x^2}{b^2} = 1$$

Standard Equation (Centre at origin)
Major axis horizontal

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

Distance from centre to focus.

$$c = \sqrt{a^2 - b^2}$$

Focal width (where a is semi-major axis)

$$L = \frac{2b^2}{a}$$

Hyperbola

Standard equation (Trans. horizontal)

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \text{slopes} = \pm \frac{b}{a}$$

Standard equation (Trans. vertical)

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1 \quad \text{slopes} = \pm \frac{a}{b}$$

Distance from centre to focus

$$c = \sqrt{a^2 + b^2}$$

Focal Width

$$L = \frac{2b^2}{a}$$