

TMTH 220
MIDTERM EXAM FORMULA SHEET

CHAPTER 15: Oblique Triangles and Vectors

Law of Sines: $\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)}$

Law of Cosines: $a^2 = b^2 + c^2 - 2bc \cos(A)$ $\cos(A) = \frac{b^2 + c^2 - a^2}{2bc}$
 $b^2 = a^2 + c^2 - 2ac \cos(B)$ $\cos(B) = \frac{a^2 + c^2 - b^2}{2ac}$
 $c^2 = a^2 + b^2 - 2ab \cos(C)$ $\cos(C) = \frac{a^2 + b^2 - c^2}{2ab}$

CHAPTER 17: Graphs of the Trigonometric Functions

General Sine Wave: $y = a \sin(bx + c)$

amplitude = $|a|$ period = $\frac{360^\circ}{b}$ or $\frac{2\pi}{b}$ frequency = $\frac{b}{360^\circ}$ or $\frac{b}{2\pi}$
phase angle = c phase shift = $-\frac{c}{b}$ $\cos \theta = \sin(\theta + 90^\circ)$

Sine wave as a function of time t: $y = a \sin(\omega t + \phi)$

amplitude = $|a|$ angular velocity = ω period = $\frac{2\pi}{\omega}$
frequency = $\frac{\omega}{2\pi}$ phase angle = ϕ phase shift = $-\frac{\phi}{\omega}$

Addition of a sine wave and cosine wave:

$A \sin \omega t + B \cos \omega t = R \sin(\omega t + \phi)$ where

$R = \sqrt{A^2 + B^2}$ and $\phi = \arctan\left(\frac{B}{A}\right)$

Transforming between Polar and Rectangular Coordinates:

$$x = r \cos \theta \quad \text{and} \quad y = r \sin \theta$$

$$r = \sqrt{x^2 + y^2} \quad \text{and} \quad \theta = \arctan\left(\frac{y}{x}\right)$$

CHAPTER 18: Trigonometric Identities and Equations

$$\cot\theta = \frac{1}{\tan\theta} \quad \sec\theta = \frac{1}{\cos\theta} \quad \csc\theta = \frac{1}{\sin\theta} \quad \tan\theta = \frac{\sin\theta}{\cos\theta} \quad \cot\theta = \frac{\cos\theta}{\sin\theta}$$

$$\sin^2\theta + \cos^2\theta = 1 \quad 1 + \tan^2\theta = \sec^2\theta \quad 1 + \cot^2\theta = \csc^2\theta$$

Sum and Difference Identities:

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \pm \tan A \tan B}$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

Double-Angle Identities:

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

$$\cos 2A = 1 - 2 \sin^2 A$$

$$\cos 2A = 2 \cos^2 A - 1$$

Function Values of Special Angles:

θ	$\sin \theta$	$\cos \theta$	$\tan \theta$	$\cot \theta$	$\sec \theta$	$\csc \theta$
30°	$\frac{\pi}{6}$ $\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{3}$ or $\frac{1}{\sqrt{3}}$	$\sqrt{3}$	$\frac{2\sqrt{3}}{3}$ or $\frac{2}{\sqrt{3}}$	2
45°	$\frac{\pi}{4}$ $\frac{\sqrt{2}}{2}$ or $\frac{1}{\sqrt{2}}$	$\frac{\sqrt{2}}{2}$ or $\frac{1}{\sqrt{2}}$	1	1	$\sqrt{2}$	$\sqrt{2}$
60°	$\frac{\pi}{3}$ $\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$	$\frac{\sqrt{3}}{3}$ or $\frac{1}{\sqrt{3}}$	2	$\frac{2\sqrt{3}}{3}$ or $\frac{2}{\sqrt{3}}$

CHAPTER 21: Complex Numbers

The Imaginary Unit: $j = \sqrt{-1}$; $j^2 = -1$; $j^3 = -j$; $j^4 = 1$; $j^5 = j$

Complex Numbers in Polar Form:

$$a + jb = r \angle \theta \quad (\text{where } r = \sqrt{a^2 + b^2} \text{ and } \theta = \arctan\left(\frac{b}{a}\right))$$

Conversion from Polar to Rectangular Form:

$$a = r \cos\theta \quad b = r \sin\theta$$

Complex Numbers in Trigonometric Form:

$$a + jb = r(\cos\theta + j \sin\theta) \quad R \angle (\omega t + \phi) = R \cos(\omega t + \phi) + R \sin(\omega t + \phi)$$